THE EFFECT OF VARIATION OF COLLISIONAL GAS PARAMETERS ON THEORETICAL ELECTROMAGNETIC TRANSIENT BREAKDOWNS

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Abstract

Prediction of the performance of intense electromagnetic transient, gaseous breakdown depends on various parameters used for the description of the gaseous media. Of these parameters, some describe the impact ionization cross section for stable atoms and molecules, and are specific for each species. These parameters are: the first ionization energy, E_i , a scaling parameter denoted as α which characterizes the collision cross section per electron volt of the species, and a parameter which represents the incident electron energy at which the peak impact ionization cross section occurs, denoted as β . This paper discusses the effect that these parameters have upon electrical breakdown performance in an intense electromagnetic transient environment.

I. INTRODUCTION

In the performance of breakdown experiments in gases subjected to intense electromagnetic transients the impact ionization cross section determines the conditions in which the ionization rate, v_i , exceeds the attachment rate , v_a , and breakdown may be expected to occur. Lupan has derived the functional dependence of the ionization rate on energy as

$$\left\langle \frac{v_i}{P} \right\rangle = \frac{N}{P} \left\langle \sigma(E) \sqrt{\frac{2E}{m_e}} \right\rangle$$
 (1)

where: P is the gas pressure, N is the gas density, E is the energy, m_e is the electron mass, and $\sigma(E)$ is the impact ionization cross section of the gas molecule. This impact ionization cross section can be approximated as¹

$$\sigma(E) = \alpha \left(E - E_i \right) e^{-\left\{ \frac{E - E_i}{\beta} \right\}} \tag{2}$$

where: E_i is the first ionization energy, α is a scaling parameter which characterizes the collision cross section per electron volt of the species, and β represents the incident electron energy at which the peak impact ionization cross section occurs. To better illustrate the definitions of these parameters, a plot of the impact ionization cross section is shown in Figure 1.

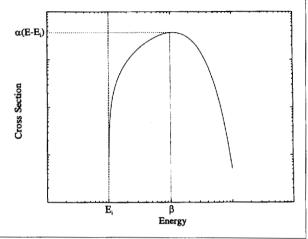


Figure 1. Cross Section vs. Energy

Prediction of the performance of intense electromagnetic transient, gaseous breakdown depends on these parameters used for the description of the gaseous media. Of these parameters, some describe the impact ionization cross section for stable atoms and molecules, and are specific for each species. Extending the method of Lupan¹ this paper discusses the effect that these parameters have upon electrical breakdown performance in an intense electromagnetic transient environment.

II. THEORY

For a maxwellian distribution function the expected value for the ionization rate becomes

$$\left\langle \frac{v_i}{P} \right\rangle = \int_{E_i}^{\infty} \frac{N}{P} \sigma(E) \sqrt{\frac{2E}{m_e}} \frac{2}{\sqrt{\pi}} \sqrt{\frac{E}{2\varepsilon}} e^{\left(\frac{-3E}{2\varepsilon}\right)} \frac{dE}{\left(\frac{2}{3}\varepsilon\right)}$$
(3)

which may be rewritten as

$$\left\langle \frac{v_i}{P} \right\rangle = \frac{3}{\sqrt{\pi}} \sqrt{\frac{3}{m_e}} \int_{E_i}^{\infty} \frac{N}{P} \sigma(E) \frac{E}{\varepsilon^{\frac{3}{2}}} e^{\left(\frac{-3E}{2\varepsilon}\right)} dE$$
 (4)

where ϵ is the free electron energy, which is the sum of the thermal energy and the kinetic energy due to the electric field

$$\varepsilon = \frac{3}{2}k_B T + \frac{\frac{1}{2}m_e \langle v(\tau)^2 \rangle}{\delta_{eff}}$$
 (5)

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and: k_B is Boltzmann's constant, T is temperature, $\langle v(\tau)^2 \rangle$ is the time average of the velocity squared over a period of au , and $\delta_{\it eff}$ is the effective fraction of energy transferred from an electron to a molecule in a collision. For an electron in an electric field the free electron energy, ε , becomes²

$$\varepsilon = \frac{3}{2}k_B T + \frac{q^2 E^2_{eff}}{m_e \delta_{eff} V^2_{eff}}$$
 (6)

where: q is the electron charge, $v_{\it eff}$ is the effective collision frequency, and $E_{\it eff}$ is the effective electric field. Combining equations and utilizing the ideal gas law produces

$$\left\langle \frac{v_i}{P} \right\rangle = \frac{3}{\sqrt{\pi}} \sqrt{\frac{3}{m_e}} \left(\frac{N}{P} \right) \int_{E_i}^{\infty} \frac{\alpha E \left(E - E_i \right) e^{-\left\{ \frac{E - E_i}{\beta} \right\}} e^{\left(\frac{-3E}{2e} \right)}}{\varepsilon^{\frac{3}{2}}} dE$$
 (7)

where R is the ideal gas law constant, T is temperature, and the effective electric field is a function of the applied electric field. For an electron at room temperature $\frac{3}{2}k_bT \approx \frac{1}{40}$ eV. Likewise the coefficients preceding the integral reduce to a value of

$$\left\langle \frac{v_i}{P} \right\rangle = \frac{3}{\sqrt{\pi}} \sqrt{\frac{3}{m_e}} \left(\frac{6.02 \times 10^{23}}{RT} \right) \int_{E_i}^{\infty} \frac{\alpha E \left(E - E_i \right) e^{-\left\{ \frac{E - E_i}{\beta} \right\}}}{\left[\frac{3}{2} k_b T + \frac{q^2 E^2_{eff}}{m_e \delta_{eff} v^2_{eff}} \right]^{\frac{3}{2}}} dE$$

Assuming that ionization is a single event process the functional dependence of the first three terms contained in the integral are estimated 1 to be, for E < 400 eV,

$$\frac{N}{P}\sigma(E)\sqrt{\frac{2E}{m_e}} = 6x 10^7 \alpha \sqrt{E}(E - E_i) \exp(\frac{E_i - E}{\beta_{N2}})$$
(9)

and for E > 400 eV.

$$\frac{N}{P}\sigma(E)\sqrt{\frac{2E}{m_e}} = \frac{6x\,10^7\,\sqrt{E}}{\sqrt{E}}\,10^2 = 6x\,10^9\tag{10}$$

Substituting the above estimates into the integral yields,

$$<\frac{v_i}{P}>=6x\,10^7\sqrt{\frac{27}{2\pi}}\,\varepsilon^{-3/2}\,[\,\alpha\,\int\limits_{E_i}^{400}E(E-E_i)\exp\{\frac{E_i-E}{\beta_{N2}}\}\exp\{\frac{-3E}{2\varepsilon}\}dt]$$

$$10^2 \int_{400}^{\infty} \sqrt{E} \exp(\frac{-3E}{2\varepsilon}) dE$$
 (12)

The left hand side of the above equation may be estimated by noting that gaseous electrical breakdown is governed by the time rate of growth of free electrons.

$$\frac{\partial n}{\partial t} = v_i n - v_a n + \nabla^2(Dn) \quad (13)$$

where n is the electron density, v_i is the ionization rate, v_a is the attachment rate, and D is electron diffusion When an electromagnetic pulse is short coefficient. compared to the diffusion time, the electron diffusion coefficient may be neglected². This allows the previous equation to be rewritten as $\frac{\partial n}{\partial t} = \Delta v n$ where $Dv = v_i - v_a$. Solving this equation, assuming Dv is not a function of

$$\ln \frac{n_f}{n_o} = \Delta v \, \tau_p \tag{14}$$

time, yields

where n_f is the final electron density, n_o is the initial electron density, and tp is the pulse length. Gould and Roberts³ established the generally recognized breakdown ratio of n_0/n_0 as 10^8 .

$$\ln 10^8 = 18.4 \approx \Delta v \, \tau_p \qquad (15)$$

For breakdown to occur it is required that $v_i >> v_a$. Thus

$$\frac{v_i}{P} = \frac{18.4}{P \tau_p} \tag{16}$$

where P is the gas pressure. Substituting the above equation into the integral, performing the integration⁴, and simplifying yields

$$\frac{18.4}{P\tau_p} = \frac{18.4}{2\pi} e^{-3/2} \exp(\frac{-3E_i}{2\varepsilon}) \left\{ \frac{16\alpha(\beta_{N2}\varepsilon)^3}{(2\varepsilon+3\beta_{N2})^3} + \frac{4\alpha(\beta_{N2}\varepsilon)^2 E_i}{(2\varepsilon+3\beta_{N2})^2} \right\}$$

$$+10^2 \sqrt{\frac{2\pi\varepsilon}{3}} \exp(\frac{3E_i - 1200}{2\varepsilon})(\frac{2\varepsilon}{3} + 800)$$
 (17)

Thus, given a knowledge of the first ionization energy E_i , the collision cross section per electron volt of the $<\frac{v_i}{P}>=6x10^7\sqrt{\frac{27}{2\pi}}\,\varepsilon^{-3/2}\left[\alpha\int_{E}^{400}E(E-E_i)\exp(\frac{E_i-E}{\beta_{ND}})\exp(\frac{-3E}{2\varepsilon})dE\right]$ species α , and the energy at which the peak impact from the energy β , one is able to generate an estimate of the Paschen Curve of a given species of gas. A tabulation of these parameters for various gases, based on the effort of McDaniel⁵, is listed in Table 1.

Table I. (Gaseous	Breakdown	Parameters
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Gas	E_{i}	α	β
H_2	13.59	2.98	70.145
He	24.59	0.029	115.8
N ₂	14.50	0.5706	108.0
O_2	13.60	0.2090	135.33
Ne	21.56	0.0310	170.2
Ar	15.76	1.128	97.4
Atomic Hydrogen	15.40	0.034	65.5
Atomic Nitrogen	15.60	0.0955	106.7
Atomic Oxygen	12.06	0.053	90.0

Figure 2 is a graph of the Paschen Curves for H₂, He, N₂, O₂, Neon, and Argon based on the values of the parameters listed in Table 1. Note that the positions of the various gases strongly correlate with the valence position of the element on the periodic chart. This positioning is to be expected since the valence position on the periodic chart is a function of the first ionization energy of an element. The nose structure occurring at approximately 10⁻⁹ Torr-seconds and 10³ Volts per centimeter per Torr has been previously predicted by Graham and Roussel-Dupre⁶ and has been experimentally observed by two of the authors⁴.

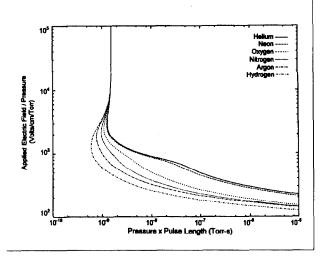


Figure 2. Paschen Curves for Various Gases

Figure 3 is a graph of the Paschen Curves for H₂, N₂, O₂, Atomic Hydrogen, Atomic Nitrogen, and Atomic Oxygen based on the values of the parameters listed in Table 1. Note the separation between the pairs of: Atomic Hydrogen and Molecular Hydrogen, Atomic Nitrogen and Molecular Nitrogen, and Atomic Oxygen and Molecular Oxygen.

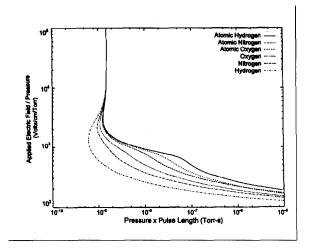


Figure 3. Paschen Curves for Molecular and Atomic Gases

Figure 4 is a graph of the Paschen Curve of a hypothetical gas with values of $\alpha = 1.0$, $\beta = 100.0$ eV, and E_i varied from 10 eV to 80 eV. As observed in Figure 2, increased ionization energy has the effect of increasing the insulating property of the gas, producing an upward shift in the Paschen Curve.

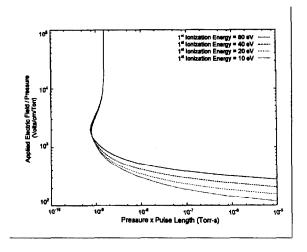


Figure 4. Hypothetical Gas, 1st Ionization Constant Varied

Figure 5 is a graph of the Paschen Curve of a hypothetical gas with values of α varied from 0.01 to 10, β =100.0 eV, and E_i = 10 eV. The α parameter adjusts the scale of the collisional cross section. Small values are indicative of relatively small collisional cross sections while large values are indicative of relatively large collisional cross sections. Larger collisional cross sections produce curves exhibiting less insulating ability while smaller collisional cross sections produce curves exhibiting more insulating ability. This is again a reasonable result since a larger collisional cross section is

easier for an electron to impact while a smaller collisional cross section is harder for an electron to impact.

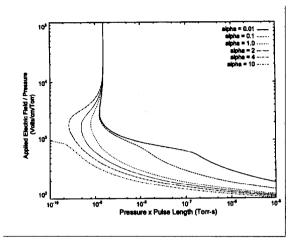


Figure 5. Hypothetical Gas, α Varied.

Figure 6 is a graph of the Paschen Curve of a hypothetical gas with values of α =1.0, β varied from 10 eV to 400 eV, and E_i = 10 eV. Note that β , the electron energy producing the peak collisional cross section, cannot be less than the first ionization constant for breakdown to occur. Note that as β increases in magnitude the nose structure of the Paschen Curve becomes more pronounced.

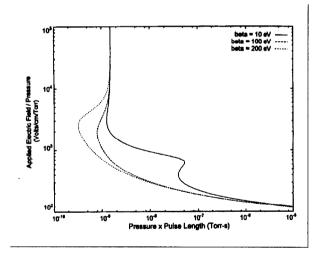


Figure 6. Hypothetical Gas, β Varied

III. CONCLUSION

This paper discusses the effect that these parameters have upon electrical breakdown performance in an intense electromagnetic transient environment. Small values of α yield relatively small collisional cross sections while large values of α yield relatively large collisional cross sections. Larger collisional cross sections produce curves exhibiting less insulating ability while smaller collisional

cross sections produce curves exhibiting more insulating ability. Large values of β , the electron energy regulating placement of the peak collisional cross section, yield more pronounced nose structures within the Paschen Curve. Finally, increased ionization energy, E_i , has the effect of increasing the insulating property of the gas, producing an upward shift in the Paschen Curve.

Given that the first ionization energy of a gas is a parameter which has been measured to a high degree of accuracy, it should be possible to determine the remaining parameters, α and β , by examination of the Paschen Curve of that gas.

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